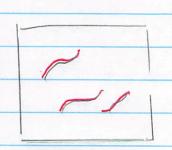
The Photon Gas



The oven glows red hot, lets calculate The number of photons in the even. See slides on next pages!

- · First note: that photons can be created and destroyed, e.g. et +e = > 8 +8 or $e \longrightarrow e + \gamma$ This will imply that $\mu = 0$ for photons
- · Since photon number is not conserved, its Chemical potential is zero. Proof:

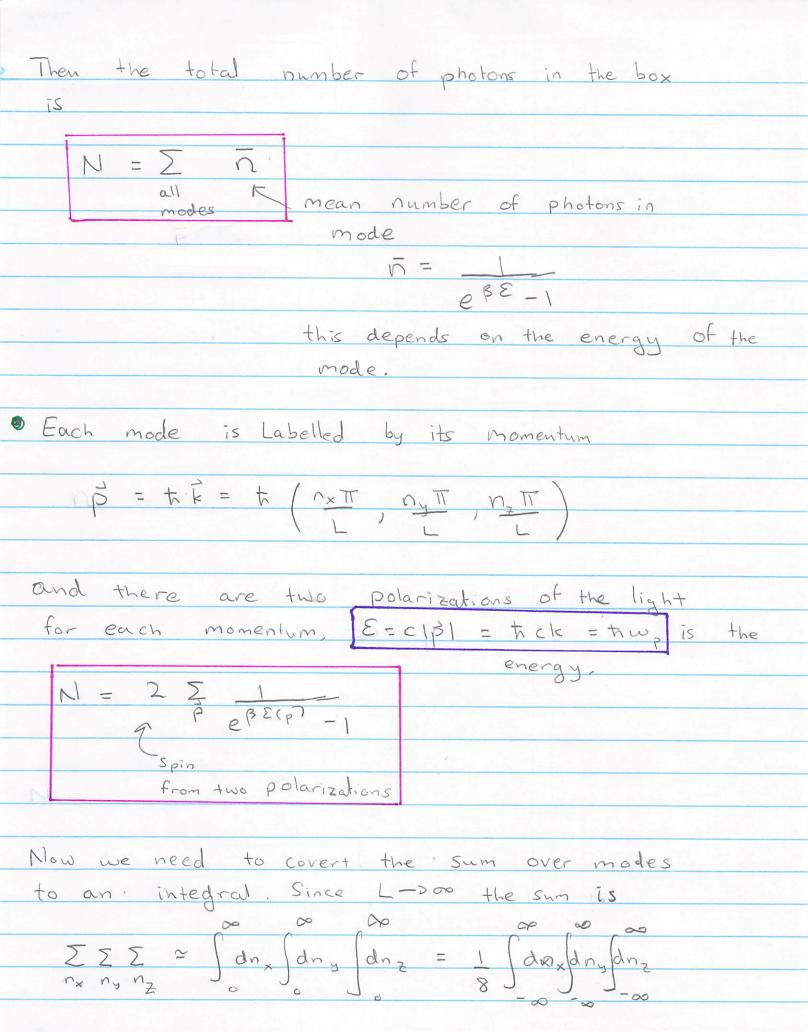
$$= \left(\frac{1}{T_1} - \frac{1}{T_2}\right) dU_1 + \mu_1 dN_1 + \mu_2 dN_2$$

In equilibrium diror = 0 so T,=Tz and M=Mz=0

Black Body Radiation and the Photon Gas:



Photons are filling the cavity. Nothing is combusting, the light is in equilibrium with the rocks. The photon gas has a certain energy per volume which we will compute as a function of temperature. This is done by calculating the mean energy per mode as a function of temperature, and then summing up the contributions from all modes.



Now
$$dn_{\times} = \left(\frac{L}{\pi t}\right) dp_{\times}$$
 Since $p_{\times} = t n_{\times}$

and similarly for x

$$\sum \sum \sum \rightarrow \int V d^3p \quad \text{or} \quad \int V d^3p$$

$$\int v_x \, v_y \, v_z \quad \int (2\pi \, t_z)^3 \, d^3p$$

There we find

$$N = 2V \int d3p \frac{1}{(2\pi + 1)^3} e^{\beta \mathcal{E}(p)} - 1$$
 where $\mathcal{E}(\vec{p}) = c|\vec{p}|$

$$U = 2 \sum_{p \in \mathcal{E}(p)} \frac{\mathcal{E}(p)}{p \mathcal{E}(p)} - 1$$

$$M = 5N \left(\frac{3^{5}}{243^{5}}\right)^{3} = 8(6)$$

E(p) = (p)

$$\int d^3p = \int p^2 dp d\Omega_p = 4\pi p^2 dp$$



Spherical

3 hell

u = p/po with po = kT/c and get This a dimensionless integral and gives 2.404=25(3) 0.244 (kBT) 3 know how to do and Such integrals you don't they will be given. J(x) is the Zeta function And $U = 2V \cdot LiT \int p^2 dp cp$ $(2T +)^3 \int e^{cp/kT-1}$ Again define po = kT/c and change variables $U = \frac{1}{T^2} \frac{V_{p_0}^3}{t^3} \frac{C_{p_0} \int \frac{u^3}{e^{\mu} - 1}}{e^{\mu} - 1}$ dimensionless integral. Can be done analytically. But not too easily

So the energy density is

$$u = U = (kT)^3 kT \cdot T^2$$
 $V = (kC)^3 kT \cdot 0.60$
 $V = (kT)^3 kT \cdot 0.60$
 $V = (kT)^3 kT \cdot 0.60$

Picture

The energy of the photon

is

E ~ KT

The Corresponding momentum

is p ~ kT Which has

wavelength = t = tc. Thus the density

of the photons is of order the

$$\frac{N}{V} = \frac{0.244}{3.3}$$

The interpaticle spacing is of order the wavelength

$$\left| \left(\frac{N}{V} \right)^{\sqrt{3}} \right| = 0.62$$